

Hardness for Explicit State Software Model Checking Benchmarks

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Abstract

Directed model checking algorithms focus computation resources in the error-prone areas of concurrent systems. The algorithms depend on some empirical analysis to report their performance gains. Recent work characterizes the hardness of models used in the analysis as an estimated number of paths in the model that contain an error. This hardness metric is computed using a stateless random walk. We show that this is not a good hardness metric because models labeled hard with a stateless random walk metric have easily discoverable errors with a stateful randomized search. We present an analysis which shows that a hardness metric based on a stateful randomized search is a tighter bound for hardness in models used to benchmark explicit state directed model checking techniques. Furthermore, we convert easy models into hard models as measured by our new metric by pushing the errors deeper in the system and manipulating the number of threads that actually manifest an error.

1 Introduction

Model checking is a formal approach for systematically exploring the behavior of a concurrent software system to verify whether the system satisfies the user specified properties [21, 13]. A model of a concurrent software system is a transition graph that consists of states and transitions. Each state in the transition graph is a snapshot of the program condition which consists of the values of all variables at a specific program location; while the transitions in the graph are rules that represent the change in the program condition from one state to another.

Exhaustive search techniques such as breadth-first search (BFS) or depth-first search (DFS) are commonly used to explore all the states in the transition graph. Starting from an initial state, the search technique computes the enabled transitions at each state to generate and explore the possible

successors in either a breadth-first or depth-first manner.

A path or state in the transition graph that violates a user specified property is known as an error in the model. Since model checking techniques consider all possible thread interactions, it enables us to find subtle concurrency errors deep in the execution trace. These errors are hard to detect in a traditional validation technique based on test vector generation because scheduling decisions cannot be controlled by the input vectors.

The primary challenge in model checking is managing the size of the transition graph. The increase in the size of the transition graph is also known as the state space explosion. For large software systems, the computation resources are exhausted before a search finishes exploring the transition graph. Directed model checking is one solution to the state space explosion problem. It aims to guide the search to parts of the transition graph where errors are more likely to exist [11, 22, 7, 26, 23]. It assumes an error exists in the software, and the goal is to find the error before it runs out of computational resources (time or memory).

Directed model checking techniques use heuristics to rank the states in order of interest with states estimated to be near errors being explored before the other states. The performance of a given heuristic estimate is compared to existing heuristic functions, or a DFS, with an empirical analysis. A reduction in the number of states generated, and a decrease in the total time taken, before error discovery are two commonly used metrics to measure performance gains of a directed model checking technique.

The reliance of directed model checking algorithms on an empirical analysis to assess and validate the performance gains of a given technique motivates a need to characterize the quality of models used in such an analysis. The set of models used to benchmark directed model checking should at least be computationally expensive for simple variants of DFS or BFS techniques. In other words, if the baseline model checking algorithm easily solves a benchmark for directed model checking, then the benchmark is not successful or useful in delineating performance. There is a need

to classify and characterize benchmarks for directed model checking to control for this situation. We believe that understanding the benchmarks improves understanding in the algorithm.

The work in [6] is the pioneering research in characterizing the hardness of benchmarks for directed model checking. The benchmarks are guaranteed to contain an error where the goal is to rank the benchmarks in terms of effort, time and memory, required for error discovery. The work in [6] presents the traditional syntactic metrics for hardness in a set of Java benchmarks such as thread count, class count, location count, etc., and it then defines a semantic hardness metric as a lower bound on the estimated number of paths in the model that contain errors. The lower bound is computed by conducting a large number of stateless random walks on the model. Follow on work in [5] shows that only 5 to 20 non-deterministic DFS trials are required to guarantee that one DFS trial successfully discovers the error. The DFS trial results are reported on a set of seven models that are classified as hard by the semantic metric for directed model checking in [6]. The results in [5] contradict the intuition that a hard model used for benchmarking directed model checking needs to minimally challenge basic search techniques and indicates that the reported lower bound on the hardness for these models in [6] is not sufficient.

To provide a semantic metric with a tighter bound on the estimated number of errors in a benchmark for explicit state directed model checking, we define a new hardness metric that is computed by conducting a large number of non-deterministic DFS trials. To test the effectiveness of this new hardness metric we conduct an analysis on a set of 36 models that have not been previously analyzed with non-deterministic DFS trials. In a large subset of the 36 models that have a low estimated number of errors as computed by random walk, all non-deterministic DFS trials conducted are successful in finding an error. The large performance gap between a random walk and non-deterministic DFS indicates that a hardness metric based on non-deterministic DFS trials is a better starting baseline measure of hardness than the one computed using random walk.

To aid researchers in designing hard benchmarks, we identify certain factors that control the hardness in models as measured by the new semantic hardness metric. Traditionally, the total number of threads is a syntactic measure of hardness used when evaluating directed model checking approaches. Our analysis indicates, however, that arbitrarily increasing the total number of threads in the model does not necessarily challenge the new hardness measure. In fact we create two versions of several models with the same number of total threads that have diametrically opposite hardness values as measured by the new metric. As such, we show that the type of threads that cause an error to be discovered and the depth at which errors occur in the transition

graph are two controlling factors that affect the hardness measure. We present evidence for these factors in making seemingly easy models into hard models by systematically varying these factors in the models.

The main contributions of this paper are:

- Defining non-deterministic DFS (randomized DFS) as a tighter bound on the hardness of a model compared to random walk.
- Showing correlation between, error discovering threads and depth of errors, and the hardness of models.
- Characterizing a set of existing benchmarks and creating hard benchmarks based on the new metric.

2 Background and Motivation

Recent work in [6] defines *path error density* as a conservative estimate on the number of paths in a model that contain an error. This estimate is a lower bound on the total number of paths that actually contain an error in the model. To compute the path error density, a large number of independent random walks are conducted on the model. The path error density is the ratio of random walks that find an error to the total number of random walks. The work in [6] also reports syntactic metrics, like lines of code and thread count, on the models used in their study. The study shows that syntactic metrics are not able to predict path error density values. A model that looks syntactically hard may actually be semantically easy. This creates a need for a semantic metric, like the path error density, to classify benchmarks for directed model checking until we better understand the relationship between syntax and error discovery.

Random walk is a stateless search technique that does not store information on states that are already explored. In Figure 1(a), we present the pseudo-code for a pure random walk with no backtracking. Starting from an initial start state (s_0), a random walk explores a sequence of states in the transition graph expanding a random successor at each state in the path (lines 8 – 14). If the random walk encounters an error it reports the error (lines 5 – 7); however, when the random walk reaches a node with no successors or a depth greater than the specified depth bound (line 9), it simply terminates the search (lines 10 and 14).

The path error density does not provide a tight bound on the number of paths in a model that contain an error due to the inherent limitations of random walk. New research in [20] shows that the total coverage obtained by a pure random walk is largely dependent on the structure of the graphs. It also shows that coverage increases logarithmically with the number of computation steps; thus, during the initial phase of the random walk, a large number of new

```

procedure Random_Walk_Init( $s_0$ )
1:  $s := s_0, depth := 0$ 
2: Random_Walk( $s, depth$ )
3:
procedure Random_Walk( $s, depth$ )
4: while ( $true$ ) do
5:   if error( $s$ ) then
6:     print “1 Error Found”
7:     exit
8:    $X_{succ} := \text{get\_successors}(s)$ 
9:   if  $|X_{succ}| = \emptyset$  or  $depth \geq depth\_bound$  then
10:    break
11:  else
12:     $s := \text{get\_random\_element}(X_{succ})$ 
13:     $depth := depth + 1$ 
14: print “No Errors on this Path”

```

(a)

```

procedure Random_DFS_Init( $s_0$ )
1:  $Visited := \{s_0\}$ 
2: Random_DFS( $s_0, Visited$ )
3:
procedure Random_DFS( $s, Visited$ )
4: if ( $\text{within\_time\_bound}()$ ) then
5:   if error( $s$ ) then
6:     print “1 Error Found”
7:     exit
8:    $X_{succ} := \text{get\_successors}(s)$ 
9:    $\text{randomize\_elements}(X_{succ})$ 
10:  for each  $s' \in X_{succ}$  do
11:    if  $s' \notin Visited$  then
12:       $Visited := Visited \cup \{s'\}$ 
13:      Random_DFS( $s', Visited$ )
14:  else
15:    print “Out of Time”

```

(b)

Figure 1. Pseudo-code for randomized search techniques (a) True random walk with no backtracking (b) DFS with a randomized transition order

states are visited, but with time, the number of newly visited states decreases rapidly. Experimental analysis indicates that the coverage achieved by pure random walk ranges between 100% to 1% for transition graphs commonly used in model checking [15, 4, 2]. In models where pure random walk achieves medium to low coverage, the path error density measure does not accurately reflect the effort required in finding an error in the model because the coverage is so sporadic.

The work in [5] shows that a parallel randomized state-space search (PRSS) is very effective in finding errors for models of [6] with relatively low path error densities. Intuitively, PRSS runs independent randomized DFS trials in parallel to discover an error. A randomized DFS is simply a variant of the rudimentary DFS that randomizes the order of its successors in the search. The PRSS approach computes the required number of nodes such that with every node running a randomized DFS trial in parallel at least one node finds the error in the model. In Figure 1(b), we present the pseudo-code for a randomized DFS. It explores a sequence of states starting from the start state (s_0), where at each state it generates a set of all possible successors, randomizes their order, and picks one successor to explore in a depth-first manner (lines 8 – 13). When the search encounters a node with no successors, it backtracks to the next node in the list of randomized successors. A randomized DFS is a stateful search technique that maintains a set of visited states to track every explored state (lines 10 – 11). The randomized DFS search terminates when an error state is encountered (lines 4 – 7) or reaches the specified time bound (lines 4 and 14 – 15). Note that the algorithm for the randomized

DFS presented in Figure 1(b) assumes that the model contains an error. Memory resources limit the amount of time a randomized DFS trial can run. Unlike a random walk, memory in a randomized DFS trial is exhausted if it is run long enough. For seven subjects presented in [6] with a relatively low path error density, the PRSS requires only between 5 to 20 nodes to guarantee error discovery in at least one randomized DFS trial [5]. This is counterintuitive since the models labeled hard seem so easy.

A hard model should at least challenge a randomized DFS which is a basic search technique used in model checking tools. It is counterintuitive for a small number of parallel randomized DFS trials in the PRSS approach to consistently discover errors in supposedly hard models. This motivates a need for defining a better notion of hardness in models for benchmarking path analyses techniques and model checking algorithms. We especially need this metric to characterize and classify benchmarks for comparative studies in explicit state directed model checking.

3 Error Density Measure

The path error density based on a stateless random walk underestimates the hardness of models for benchmarking stateful directed model checking algorithms. Specifically, it tends to label models hard even when the error discovery is trivial with a stateful randomized DFS. A hard model used for benchmarking directed model checking algorithms needs to at least be computationally expensive in terms of time and space for a stateful randomized DFS. To demonstrate the utility of having a stateful hardness measure, we

re-run the PRSS analysis for 36 models in [6] that have not been previously analyzed with the PRSS approach in [5]; however, instead of computing the number of nodes required to run randomized DFS in parallel to guarantee at least one node finds an error, we record the number of randomized DFS trials that encounter an error.

Based on randomized DFS trials, we define a new hardness metric, the observed randomized-DFS (R-DFS) error density which is the ratio of the randomized DFS trials that find an error to the total number of randomized DFS trials conducted. Since the observed R-DFS error density is based on a stateful search, it provides a tighter bound on the hardness of models for benchmarking explicit state directed model checking algorithms compared to path error density which is computed using random walk. The underlying assumption is that randomized DFS always achieves better coverage of a transition graph compared to a random walk.

3.1 Experiment Design

To compare path error density and observed R-DFS error density we conduct random walk and randomized DFS trials on a cluster of 618 nodes. Every node in the cluster has 8 GB of RAM and two Dual-core Intel Xeon EM64T processors (2.6 GHz). The execution time for a single randomized DFS trial is bounded at one hour. We pick the time bound to be consistent with the other recent studies [6, 5]. Later in this section we also study the affects of changing the time bound. The programs in this study are compiled using Java 1.5 and verified by the Java PathFinder (JPF) v4.0 model checker with partial order reduction turned on [27].

For each model in test we conduct 100 randomized DFS trials to compute its semantic hardness. We experimented with different number of trials to pick an upper bound on the required number of trials for predicting the semantic hardness. For the models in our test suite we found that 100 trials are sufficient to compute the semantic hardness. To compute the path error density, we execute 10,000 trials of random walk, where one trial is a single random walk execution or single path in the program. The original study of [6] uses between 1000 and 10,000 random walk trials to estimate the path error density of the model.

3.1.1 Independent Variable

We vary models, the independent variable, in our study to test whether randomized DFS provides a tighter bound on hardness of benchmarks used in explicit state directed model checking. We conduct the study on a set of 36 models used in the benchmarking analysis of [6] and have not been previously analyzed with a randomized DFS. The set of benchmarks encompasses a wide variety of Java programs

with concurrency errors. The test suite includes programs derived from concurrency literature, small to medium-sized realistic programs, models designed to exhibit Java-specific errors described in [10], and models developed at IBM to support their analyses research [9]. Many models have been made parameterizable to control the number of threads for studying their effect on the path error density.

3.1.2 Dependent Variables and Measures

The dependent variables in this study are the path error density and the observed R-DFS error density values. We compute the values of the path error density rather than report the values in [6]¹. We also compute the observed R-DFS error density which is the ratio of randomized DFS trials that find an error over the total number of randomized DFS trials executed. On the scale of hardness, an observed R-DFS error density of 1.00 indicates an extremely easy model while an observed R-DFS error density of 0.00 indicates a very hard model. We measure the number of states generated during the randomized DFS trials to gain a better understanding on the effort required for error discovery by the randomized DFS trials in terms of time and memory resources.

3.2 Results

The results of the study are presented in Table 1 where the first column indicates the name of the subject, and the maximum number of threads created in the subject is indicated in the parenthesis (*Name(Thread Num)*). The second column specifies the input parameters (*Params*) used by the subject (see [6] for parameter details and other syntactic metrics such as thread count, class count, location count, etc.). In the section of Table 1 labeled *randomized DFS trials*, we present four statistics: the *observed R-DFS error density*, the *minimum* and *maximum* number of states generated in a single trial of randomized DFS among the error discovering trials, and the *average* number of states generated across all randomized DFS trials that find an error.

The analysis in Table 1 shows that for a large number of models that have near zero path error densities with random walk, almost all of the randomized DFS trials find an error. For example, the model `Clean` with parameters (1,1,12) has a path error density of 0.033 while its observed R-DFS error density is 1.00. The parameterized versions of the `TwoStage` and `Reorder` models have a path error density of less than 0.050 but have an observed R-DFS error density of 1.00. In 26 examples presented in Table 1 out of the total 36 subjects, all 100 trials of randomized DFS find an error. Furthermore, in some models with a low path error density

¹The values in [6] are computed on JPF3.1.2 while we do our analysis on JPF4.0.

Table 1. Comparing path error density and randomized DFS

Subject			Randomized DFS trials			
Name(Thread Num)	Params	Path error density[6]	observed R-DFS error density	Number of States		
				Minimum	Average	Maximum
ProducerConsumer(11)	2,8,4	0.967	1.00	127	261	12,334
ProducerConsumer(7)	2,4,4	0.956	1.00	97	116	372
ReplicatedWorkers(9)	8,2,0,10,.001	0.948	0.97	1,739	1,801	1,866
RWNoExcepChk(5)	2,2,100	0.769	0.80	52	533	2,031
ProducerConsumer(5)	2,2,4	0.768	1.00	93	112	210
Account-NoDeadlkCk(6)	none	0.549	1.00	182	27,928	1,089,171
WrongLock(12)	10,1	0.478	1.00	61	94	167
Deadlock(3)	1	0.450	1.00	12	17	33
AllocateVector(3)	8,20,1	0.441	0.99	33	198,206	4,623,001
Deadlock(3)	2	0.379	1.00	5	6	8
AllocateVector(3)	2,20,4	0.294	1.00	34	5,646	143,866
Clean(21)	10,10,1	0.289	0.96	206	283,357	5,497,056
WrongLock(12)	1,10	0.200	1.00	25	1,574,058	2,966,459
Deos(4)	abstracted	0.190	1.00	7	747	2,638
AccountSubtype(10)	8,1	0.152	0.34	250	248,714	3,245,340
RaxExtended(6)	2,3	0.128	1.00	25	1,783	19,502
Alarm Clock(4)	9	0.093	1.00	28	112	288
AllocateVector(3)	2,20,1	0.084	1.00	34	4,832	7,773
Alarm Clock(4)	4	0.083	1.00	41	111	147
Piper(17)	2,8,4	0.083	0.96	146	621,340	7,921,766
Account-NoExcpCk(6)	none	0.077	0.48	405	1,749,259	13,151,326
Airline(21)	20,8	0.069	0.49	101	571,214	6,479,374
WrongLock(3)	1,1	0.068	1.00	13	25	43
TwoStage(3)	1,1	0.043	1.00	20	57	127
Reorder(7)	1,5	0.043	1.00	15	49,151	65,490
Clean(3)	1,1,12	0.033	1.00	12	907	987
Reorder(3)	1,1	0.030	1.00	16	55	80
Airline(7)	6,2	0.030	1.00	40	226,846	5,112,586
Piper(9)	2,4,4	0.029	1.00	1,611	189,872	1,288,076
TwoStage(8)	2,5	0.028	1.00	30	1,759,759	3,702,115
TwoStage(5)	2,2	0.022	1.00	34	3,301	8,638
AllocateVector(3)	2,100,1	0.017	1.00	34	28,406	40,248
Airline(7)	6,1	0.003	1.00	50	1,618,915	6,401,539
Piper(33)	2,16,8	0.001	0.00	-	-	-
Airline(21)	20,2	0.000	0.01	5,249	5,249	5,249
LinkedListSync(5)	4,100	0.000	1.00	9,324	10,014	12,351

and high observed R-DFS error density, the minimum and average number of states generated in the randomized trials is very small. This indicates that the computation cost in terms of memory for error discovery in these models is very low. Fourteen models with an observed R-DFS error density of 1.00 generate less than 1000 average states before error discovery. In fact, some models like `TwoStage` with parameters (1,1) and `ProducerConsumer` with parameters (2,4,4) generate a maximum of only 127 states and 372 states respectively in a single randomized DFS trial out of the 100 trials. This further shows for these models that a stateful search technique is effective in finding an error when compared to random walk.

The fact that most models have a hardness of 1.00 under the observed R-DFS error density metric shows that the set of models used in [6] severely lacks in diversity when evaluating directed model checking approaches. It also indicates that the more varied distribution of hardness values computed by the path error density in [6] is not representative of the amount of effort required to find errors in these models with stateful search methods.

The examples in Table 1 that appear hard in terms of the observed R-DFS error density are interesting to study in order to identify factors that cause a low observed R-DFS error density in the models. For example, the `AccountSubtype` model with parameters (8,1) is a moderately hard model with an observed R-DFS error density of 0.34, and the average number of states generated before error discovery is significant. Further examination of the `AccountSubtype` model may assist in identifying the factors affecting the low observed R-DFS error density. There are two other parameterized subjects that have a low observed R-DFS error density: `Airline` with parameters (20,2) and `Piper` with parameters (2,16,8). These are interesting subjects because other parameterized versions of these models have a high observed R-DFS error density. For example, `Piper` with parameters (2,4,4) and `Airline` with parameters (6,1) have an observed R-DFS error density of 1.00. These models may help us in understanding hardness in explicit state directed model checking benchmarks since their hardness is not tied to syntactic metrics in any obvious manner.

3.3 Effect of the Time Bound

The observed R-DFS error density measure in Table 1 is dependent on the time bound of 1 hour set for the randomized DFS trials. We test the affect of the time bound on the observed R-DFS error density by running randomized DFS trials on a set of hard models using different time bounds. In the next section we show how to create the hard models. The independent variable in this study is the time bound while the dependent variable is the observed R-DFS error density. We expect the observed R-DFS error density to increase with the time bound. In Table 2 we present results of the study.

Table 2. Increasing Time Bound

Subject		observed R-DFS error density		
Name (Thread Num)	Params	1 hour	2 hours	3 hours
Airline(21)	20,2	0.01	0.00	0.00
Reorder(11)	9,1	0.06	0.45	0.37
TwoStage(9)	7,1	0.41	0.69	0.93
TwoStage(10)	8,1	0.04	0.03	0.07
TwoStage(12)	10,1	0.00	0.00	0.00
Wronglock(22)	1,20	0.18	0.20	0.20

In certain models, the observed R-DFS error density steadily increases with time while in others, the observed R-DFS error density does not change statistically. In the `TwoStage` model with parameters (7,1), the observed R-DFS error density increases from 0.41 to 0.93. This still shows that `Twostage(7,1)` is a moderately hard model for stateful search techniques because it takes an upper bound of 300 computation hours—a significant amount of resources—to obtain an observed R-DFS error density of 0.93 in the model. In essence, the time bound allows researchers to set their own threshold of hardness. A decrease in time bound makes a model progressively harder and vice-versa which shows that the time bound contributes towards the hardness of the model.

3.4 Summary

The effectiveness of the randomized DFS trials in error discovery indicates that the observed R-DFS error density improves over random walk to measure hardness of models used in benchmarking directed model checking techniques. In the following section, we use models defined as hard in terms of the observed R-DFS error density measure to identify the factors that contribute toward hardness other than the time bound. In other words, given a fixed time bound, how do we make an easy model hard? Based on our prior experience with models in C [23] and the experimental analysis in this paper, we show that the number of threads that manifest an error in the model and the depth of the transition

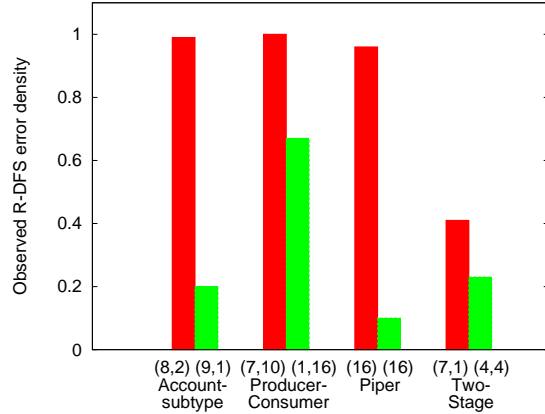


Figure 2. Same thread count in a model yields different hardness results

graph at which errors occur assist in making hard models. We also use these factors to convert some easy models into hard models in a given time bound.

4 Controlling Factors for Hardness

The total thread count in a model is not a good indicator of its hardness based on our new metric. Even though the state space of the model grows exponentially with an increase in the total number of threads in the model it does not necessarily make it harder for randomized DFS to find the errors. In Figure 2 we show two versions of four different models. The two versions of each model have the same total number of threads; however, one version is extremely easy with a high observed R-DFS error density while the other version is hard with a low observed R-DFS error density. For example, the model `Accountsubtype` with the parameters (8,2) and (9,1) have an observed R-DFS error density of 0.20 and 0.99 respectively. We observe a similar disparity in observed R-DFS error density for the other models in Figure 2. Simply increasing threads or concurrency does not reduce the number of errors in the model which motivates a need to identify other factors that affect hardness in models.

In an empirical study in this section we show that the number of threads that actually manifest an error in the model and the depth of the errors are the controlling factors of hardness in models based on the new metric. The empirical study in this section uses the same experiment design described in the previous section for Table 1; however, we specifically vary models in this study based on the control-

Table 3. Summary of Models made hard

Subject	(Params) : Making models Hard
Accountsubtype	(#correctAccounts , #incorrectAccounts) : We increase the number of threads that create #correctAccounts and keep the number of threads that create #incorrectAccounts constant because only threads that create #incorrectAccounts cause an error condition.
Wronglock	(#dataLockers , #classLockers) : We increase the #classLockers while keeping the #dataLockers constant; dataLockers check for the data inconsistency created by classLockers .
ProducerConsumer	(#producers , #consumers , #items) : We increase #consumers and keep #producers constant because the error condition, deadlocked consumer threads, is detected after the correctly running consumer threads complete execution.
Reorder	(#setters , #checkers) : We increase the #setters and keep #checkers constant; setter threads create the error while checker threads manifest the error.
TwoStage	(#twoStagers , #readers) : We increase the #twoStagers and keep #readers constant; twoStager threads cause the error while reader threads manifest the error.
Piper	(#seatRequests , #producers and #consumers , bufferSize) : Errors are pushed deeper in the transition graph when we increase the bufferSize and keep the number of threads, #producers and #consumers , constant.
Airline	(#ticketsIssued , cushion) : The minimum depth of the error is pushed deeper in the execution trace when we increase the value of cushion and keep the total possible number of threads, #ticketsIssued , constant.

ling factors. Finally, we compute the observed R-DFS error density, number of states generated and error depth statistics which are the dependent variables and measures in this study.

A summary of the subset of models made hard using the controlling factors is presented in Table 3. We are still working on other models from the study. In Table 4 we present evidence of the factors by making models hard using these factors. We present in Table 4 the *observed R-DFS error density*, the minimum (*Min*), maximum (*Max*), and average (*Average*) number of states generated, and the minimum (*Min*), maximum (*Max*) and average (*Average*) depth of errors observed during the randomized DFS trials.

4.1 Specific Thread type

The type and number of threads that actually manifest an error is a key factor in determining the hardness of the model. In the `Accountsubtype` model there are two kind of threads where one type of thread creates error-free accounts and the other creates error-causing accounts. In this example, the amount of effort required to find an error in the model depends on the number of threads that create error-causing accounts. If there is a large number of error-causing accounts, the total number of errors in the model increases and this causes a high observed R-DFS error density of the model. If we specifically decrease the number of threads that manifest an error in the model we can design hard benchmarks for directed model checking. To test this hypothesis, in the `Accountsubtype` model we increase the number of threads that create error-free accounts from 9 to 20 while fixing the number of threads that create error-

causing accounts at 1, the corresponding observed R-DFS error density value drops from 0.20 to 0.00 as shown in Table 4. In contrast, when we fix the number of threads that create error-free accounts at 8 while increasing the number of threads that create error-causing accounts from 1 to 8, the observed R-DFS error density value dramatically increases from 0.34 for parameters (8,1) seen in Table 1 to an observed R-DFS error density of 1.00 for parameters (8,8) as seen in Table 4. As described in Table 3, we manipulate the type of threads that manifest an error in the `Wronglock`, `ProducerConsumer`, `Reorder`, and `TwoStage` models to create hard models. The results on the observed R-DFS error density are shown in Table 4.

4.2 Depth of Errors

Another important factor that controls the hardness in models is the depth of errors in the transition graph. The hardness in the `Piper` and `Airline` models is controlled by varying the depth of the error for a specific thread configuration. The `Piper` model with parameters (2,4,4) has a moderately-deep distribution of errors as seen in Figure 3. The depth of errors in the `Piper` model can be controlled by increasing the size of the global buffer as described in Table 3. This is because a larger buffer requires more execution steps in the transition graph to fill the buffer. The `Piper` model with parameters (2,8,5) and 17 threads has an observed R-DFS error density of 0.59 as shown in Table 4. If we fix the number of threads and increase the buffer size from 5 to 7, the corresponding observed R-DFS error density rapidly drops to 0.01. The minimum depth of the errors also dramatically increases as shown in Table 4. A strong

Table 4. Making models hard as measured by the observed R-DFS error density

Subject Name(Thread Num)	Params	observed R-DFS error density	States			Error Depth Statistics		
			Min	Average	Max	Min	Average	Max
Accountsubtype(17)	8,8	1.00	541	569	1526	540	558	575
Accountsubtype(11)	8,2	0.99	294	66798	6297122	281	305	319
Accountsubtype(11)	9,1	0.20	281	115200	1149916	275	282	293
Accountsubtype(12)	10,1	0.19	309	404441	5045723	302	311	321
Accountsubtype(13)	11,1	0.13	332	5471	37580	331	339	347
Accountsubtype(22)	20,1	0.00	-	-	-	-	-	-
Wronglock(22)	1,20	0.18	26	42	69	25	41	68
ProducerConsumer(10)	1,8,4	0.97	92	177838	4651467	90	107	128
ProducerConsumer(12)	1,10,4	0.73	100	120234	2099605	99	117	135
ProducerConsumer(14)	1,12,4	0.74	111	226531	4352859	110	128	153
ProducerConsumer(18)	1,16,4	0.67	128	42657	2741804	127	147	173
Reorder(7)	5,1	1.00	3411	23412	34573	33	38	47
Reorder(10)	8,1	1.00	460500	2753141	4324228	46	55	66
Reorder(11)	9,1	0.06	5228089	6024276	6928518	57	61	63
Reorder(12)	10,1	0.00	-	-	-	-	-	-
TwoStage(8)	6,1	1.00	57080	1566880	3889834	53	60	69
TwoStage(9)	7,1	0.41	330917	5534023	9472266	63	68	73
TwoStage(10)	8,1	0.04	4412764	6454082	8350644	75	76	76
TwoStage(12)	10,1	0.00	-	-	-	-	-	-
Piper(17)	2,8,5	0.59	152	3100522	8611433	143	150	164
Piper(17)	2,8,6	0.10	160	2825817	7200552	141	147	159
Piper(17)	2,8,7	0.01	7016824	7016824	7016824	144	144	144
Airline(21)	20,7	0.30	116	881910	8120367	109	118	123
Airline(21)	20,6	0.19	166	233024	2936562	117	120	122
Airline(21)	20,5	0.10	183	497437	2716582	113	120	122
Airline(21)	20,4	0.03	26404	946680	2092517	118	121	123
Airline(21)	20,3	0.01	2839090	2839090	2839090	120	120	120
Airline(21)	20,1	0.00	-	-	-	-	-	-

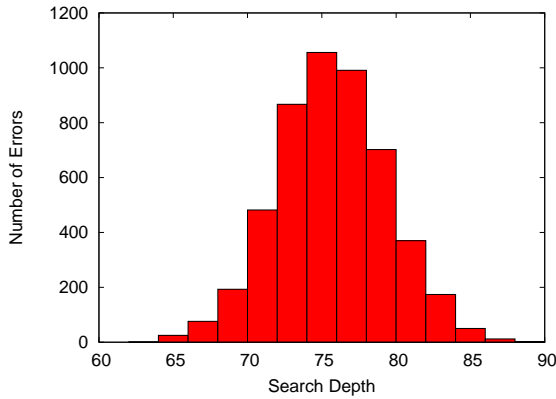


Figure 3. Distribution of error depths for the Piper model with parameters 2,4,4

dependence on the depth of errors in the Piper model allows us to create hard versions of the Piper model in terms of the observed R-DFS error density. The Airline model is made hard in the same fashion as described in Table 3. By controlling the value of the **cushion** parameter the Airline models with 21 threads get progressively harder as shown in Table 4.

4.3 Summary

Most models in Table 3 challenge a time-bounded randomized DFS and are suitable for studying directed model checking algorithms. We also show that the number of threads that manifest an error and the depth of errors are two factors that control the hardness in the models. These factors can be used to design hard benchmarks for directed model checking.

5 Threats to Validity

Since path error density [6] and observed R-DFS error density are semantic based hardness measures, the computed values are dependent on the implementation of the tool. In fact, a simple comparison between two versions of JPF shows that the hardness measures also change in different versions of the same tool. There are even a few models

where the hardness is reversed in the two versions of the tool; a model is hard in one version of the tool and easy in the other. This indicates that the models need to be characterized for a specific tool before being used to evaluate the directed model checking techniques in the tool. Differences in the implementations of partial order reduction, symmetry reduction, and state storage techniques across tools and tool versions might cause the variance in semantic measures of hardness. Despite the implementation differences, the observed R-DFS error density provides a tighter bound on the hardness of the model compared to path error density in a given tool.

6 Related Work

In recent years tremendous progress has been made in the field of software model checking [1, 14, 3, 15]. Java Pathfinder model checks the actual Java bytecode using a Java virtual machine [27]. Similar approaches use simulators and debuggers for other machine architectures [18, 19]. These approaches retain a high-fidelity model of the target execution platform while retaining a low-level control of scheduling decisions. There is a growing interest in developing tools and models for benchmarking different model checking approaches used to verify multi-threaded programs [8, 9, 10]. Recent work [6] makes a good first attempt in trying to evaluate the hardness of models used for benchmarking directed model checking by using random walk to estimate the number of paths in a model that contain an error. It is the first time random walk is used to evaluate the quality of directed model checking benchmarks. Other researchers have often used variants of random walk as an error discovery mechanism with limited success [12, 24, 17, 20].

Randomization techniques have been used in tandem with different model checking approaches by various researchers. Stoller uses randomized scheduling to find thread interactions that lead to an error in Java programs [25], while Jones and Mercer randomize a decentralized parallel guided search to disperse the search in different parts of the transition graph [16]. The work in [6] shows that the default search order used by an algorithm in a model significantly affects the results for error discovery in empirical analysis. The analysis in [6] demonstrates that by simply randomizing the default search order, the same algorithm may perform worse than other algorithms. The PRSS approach in [5] overcomes the limitations of the default search order by using a depth-first search that randomizes the order of successors.

7 Conclusions and Future Work

Characterized and classified experimental benchmarks for directed model checking are critical to understand the performance in explicit state directed model checking. Currently, we do not have the syntactic metrics for this classification and characterization. As such, this paper defines the observed R-DFS error density as a semantic metric suitable for directed model checking empirical studies. The observed R-DFS error density is based on a rudimentary search technique and provides a lower bound on the number of errors in a model. Our analysis in this paper of the most comprehensive benchmark set of Java programs for explicit state directed model checking shows the set to be lacking in diversity and hardness. We study the few Java models that have a low observed R-DFS error density to understand the factors that contribute toward making them hard. Our analysis of the hard models seems to indicate that a model can be made hard by pushing errors deep in the transition graph and manipulating the thread count of specific threads reducing the number of errors. We use these factors to systematically lower the observed R-DFS error density of several easy models.

In future work, we want to identify additional factors that affect the observed R-DFS error density of a model and tie those factors to syntactic constructs in the model. Some interesting factors to study are the depths of the transition graph where the randomized DFS spends a large portion of its search time and the structure of the transition graph derived from the branching factor. Another avenue for interesting future work is characterizing patterns in the models that render certain models hard for a specific directed model checking algorithm. This is useful for practical application of model checking in the field where a heuristic must be selected for a given model and property.

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